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Carathéodory-type Results for Faces of Convex Sets

We present several Carathéodory-type results on extreme representations of sums and unions of finitely many closed convex sets or polyhedra in  $\mathbb{R}^n$  in terms of their faces. For example, if  $K_1, \ldots, K_r$  are nonempty line-free closed convex sets in  $\mathbb{R}^n$ , then for any point  $z \in K_1 + \cdots + K_r$ , there are nonempty faces  $F_i$  of  $K_i$ ,  $i = 1, \ldots, r$ , such that  $z \in F_1 + \cdots + F_r$  and the sum of dimensions of these faces does not exceed n. (This is a joint work with Jim Lawrence.)